

FIG. 1

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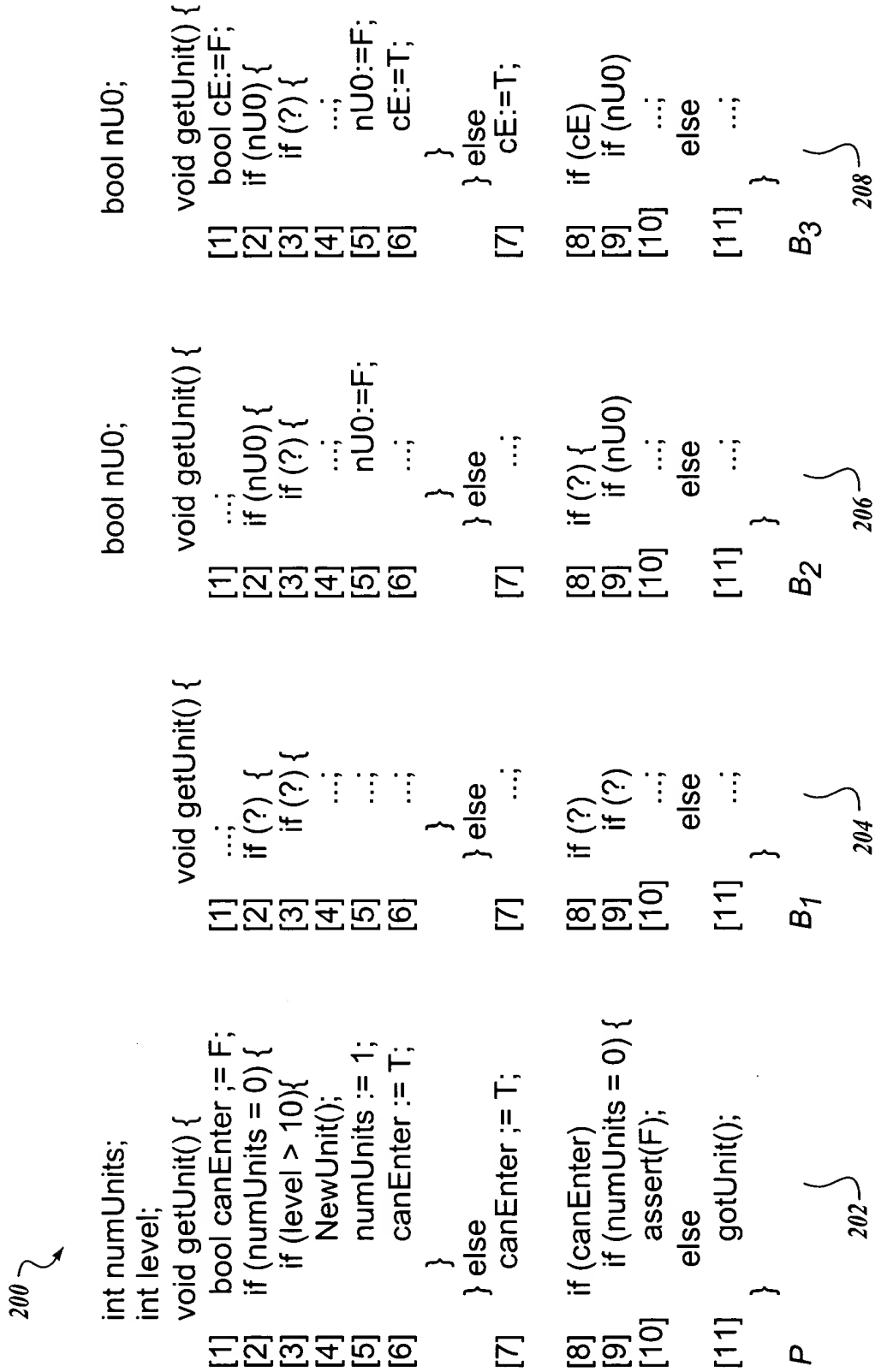


FIG. 2

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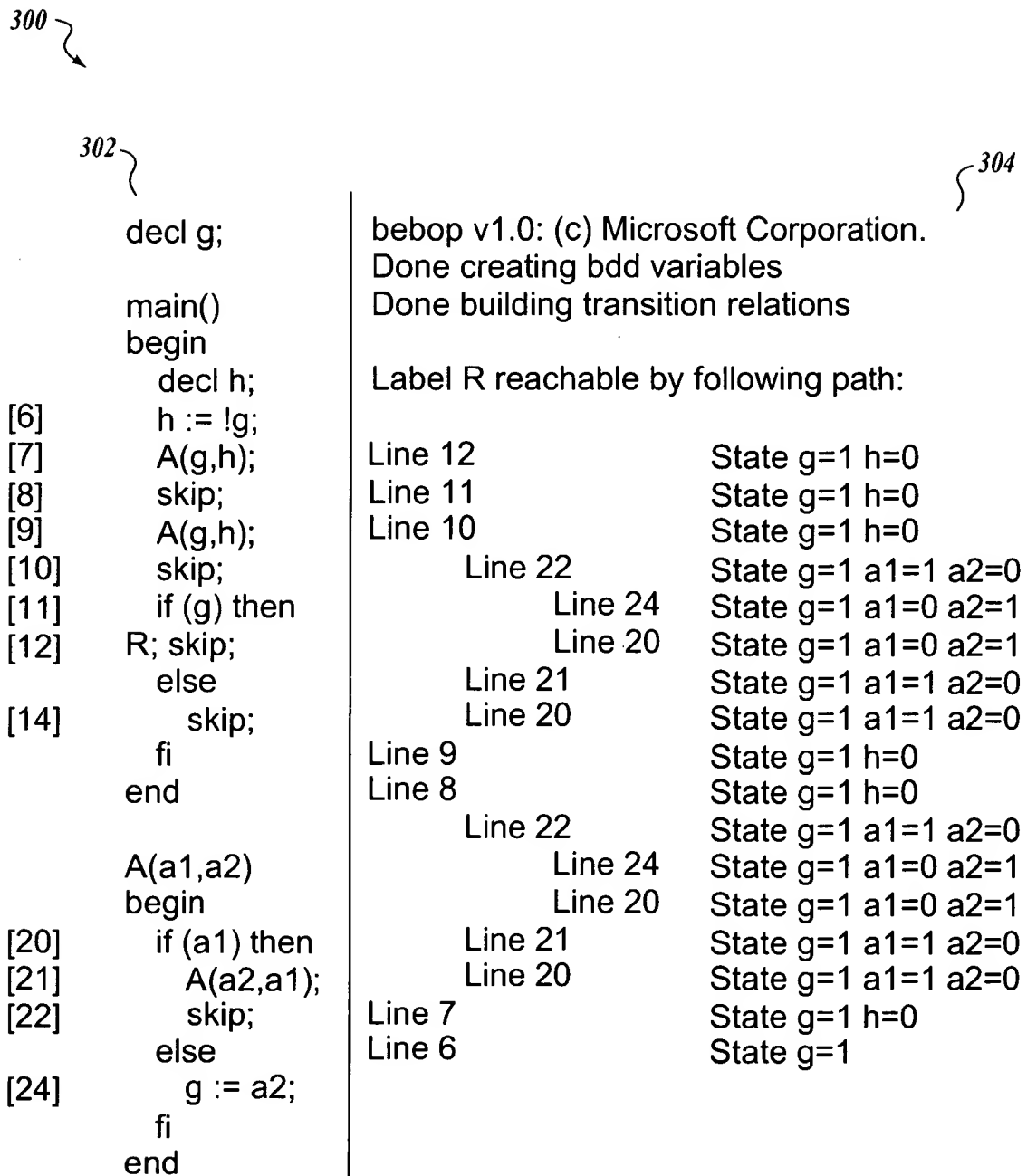


FIG. 3

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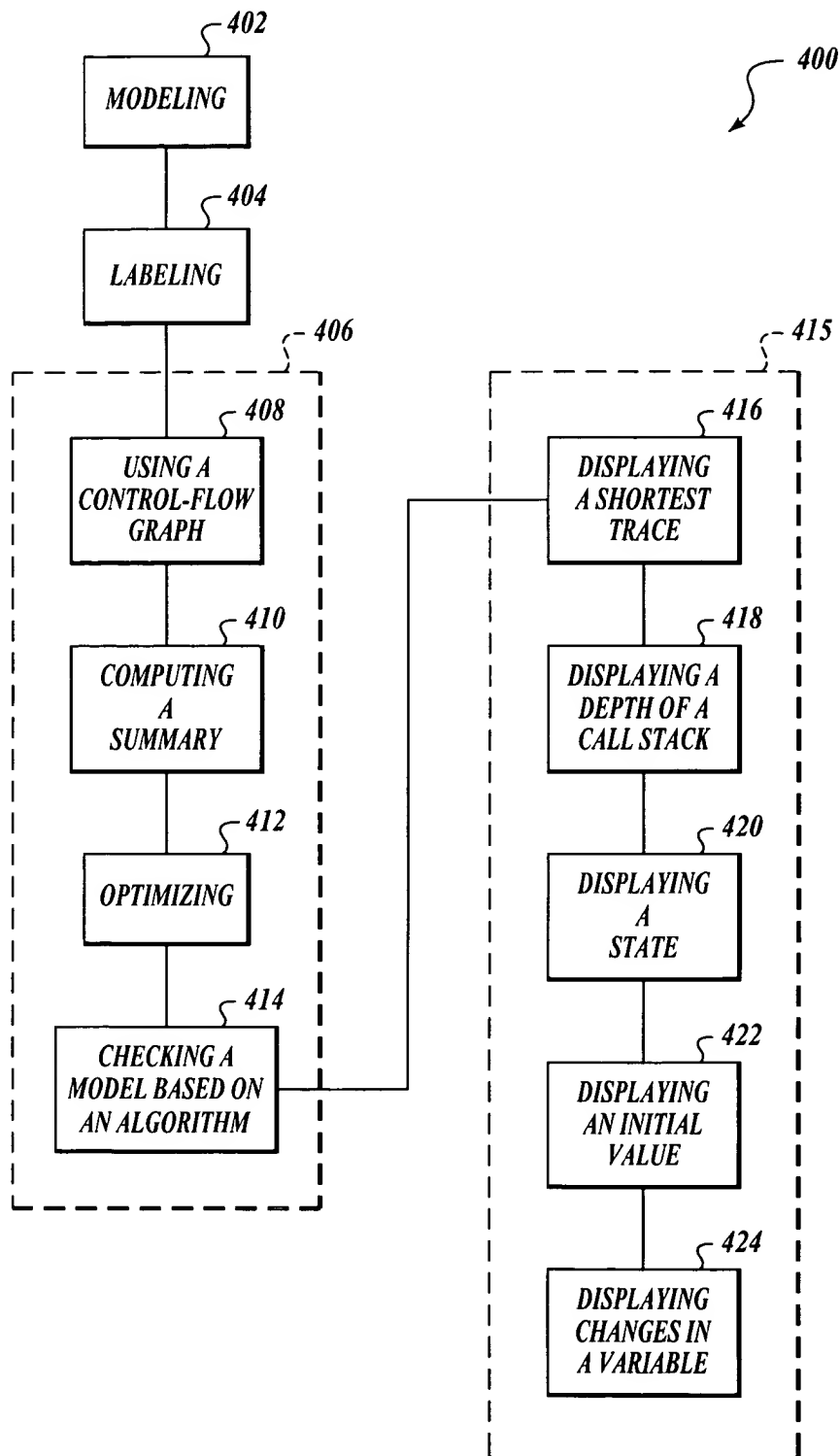


FIG. 4

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```

[1]   if (z) {
[2]       x:=1;
      else
[3]       x:=z;
[4]       z:=y|x;

```

FIG. 5A

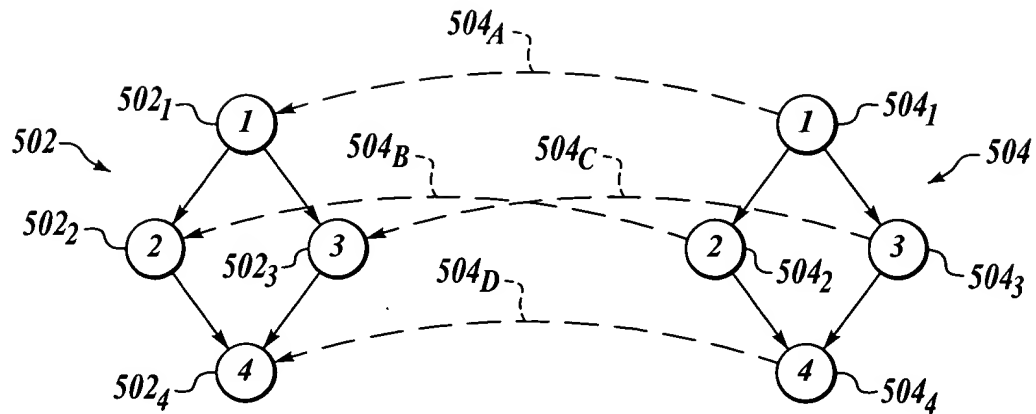


FIG. 5B

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```
Boolean g;  
[1] main() {  
[2]     if (z) {  
[3]         x:=1;  
[4]     else  
[5]         x:=0;  
  
[6]     z:=y+x;  
  
[7]     foo (z);  
[8]     skip;  
[9] }  
  
[10] foo (z) {  
[11]     g:=1;  
[12] }
```

FIG. 6A

602

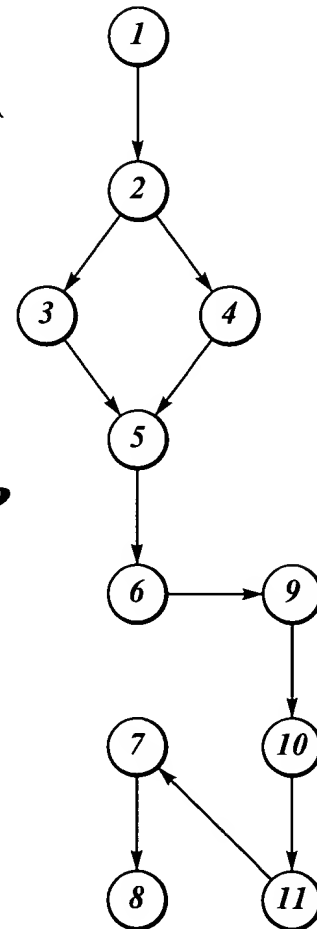


FIG. 6B

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ν	$Transfer_{\nu}$
skip print goto return	$\lambda\langle\Omega_1, \Omega_2\rangle.(\Omega_2 = \Omega_1)$
$x_1, \dots, x_k :=$ e_1, \dots, e_k	$\lambda\langle\Omega_1, \Omega_2\rangle.(\Omega_2 = \Omega_1[x_1/\Omega_1(e_1)] \dots [x_k/\Omega_1(e_k)])$
if(d) while(d) assert(d)	$Transfer_{\nu, true} = \lambda\langle\Omega_1, \Omega_2\rangle.((\Omega_1(d) = 1) \wedge (\Omega_2 = \Omega_1))$ $Transfer_{\nu, false} = \lambda\langle\Omega_1, \Omega_2\rangle.((\Omega_1(d) = 0) \wedge (\Omega_2 = \Omega_1))$
pr(e_1, \dots, e_k)	$\lambda\langle\Omega_1, \Omega_2\rangle.(\Omega_2 = \Omega_1[x_1/\Omega_1(e_1)] \dots [x_k/\Omega_1(e_k)])$, where x_1, \dots, x_k are the formal parameters of pr

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FIG. 7

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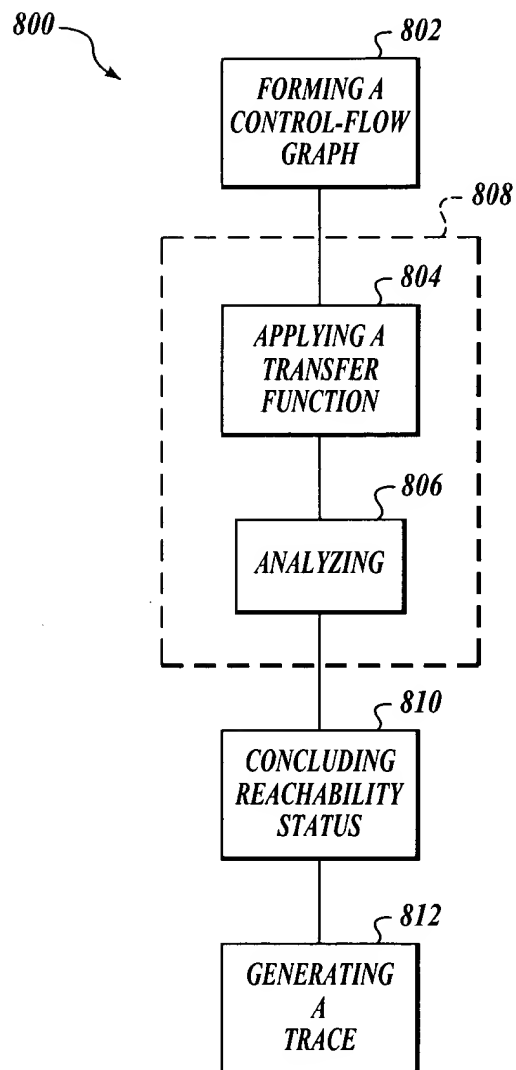


FIG. 8

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```

902 ~ global
    PathEdges, SummaryEdges, WorkList
904 ~ procedure Propagate(v,p)
    begin
906 ~   if  $p \not\subset \text{PathEdges}(v)$  then
908 ~      $\text{PathEdges}(v) := \text{PathEdges}(v) \cup p$ 
910 ~     Insert  $v$  into WorkList fi
    fi
912 ~ end

914 ~ procedure Reachable( $G_B$ )
    begin
916 ~   for all  $v \in V_B$  do  $\text{PathEdges}(v) := \{\}$ 
917 ~   for all  $v \in \text{Call}_B$  do  $\text{SummaryEdges}(v) := \{\}$ 
918 ~    $\text{PathEdges}(\text{First}_B(\text{main})) :=$ 
         $\{\langle \Omega, \Omega \rangle \mid \Omega \text{ is any valuation to globals and local variables of } \text{main} \}$ 
920 ~    $\text{WorkList} := \{\text{First}_B(\text{main})\}$ 
922 ~   while  $\text{WorkList} \neq 0$  do
924 ~     remove vertex  $v$  from WorkList
926 ~     switch ( $v$ )
928 ~       case  $v \in \text{Call}_B$ 
          Propagate( $\text{Succ}_B(v), \text{SelfLoop}(\text{Join}(\text{PathEdges}(v), \text{Transfer}_v))$ ) ~ 930
          Propagate( $\text{ReturnPt}_B(v), \text{Join}(\text{PathEdges}(v), \text{SummaryEdges}(v))$ ) ~ 932
934 ~       case  $v \in \text{Exit}_B$ :
          for each  $w \in \text{Succ}_B(v)$  do ~ 936
            let
               $c \in \text{Call}_B$  such that  $w = \text{ReturnPt}_B(c)$  and ~ 938
               $s = \text{Lift}_c(\text{PathEdges}(v), \text{ProcOf}_B(v))$  ~ 940
            in
              if  $s \not\subset \text{SummaryEdges}(c)$  then ~ 944
                 $\text{SummaryEdges}(c) := \text{SummaryEdges}(c) \cup s$  ~ 946
                Propagate( $w, \text{Join}(\text{PathEdges}(c), \text{SummaryEdges}(c))$ ); ~ 948
              ni
950 ~       case  $v \in \text{Cond}_B$ :
          Propagate( $\text{Tsucc}_B(v), \text{Join}(\text{PathEdges}(v), \text{Transfer}_v, \text{true})$ ) ~ 952
          Propagate( $\text{Fsucc}_B(v), \text{Join}(\text{PathEdges}(v), \text{Transfer}_v, \text{false})$ ) ~ 954
956 ~       case  $v \in V_B - \text{Call}_B - \text{Exit}_B - \text{Cond}_B$ :
          let  $p = \text{Join}(\text{PathEdges}(v), \text{Transfer}_v)$  in ~ 958
          for each  $w \in \text{Succ}_B(v)$  do ~ 960
            Propagate( $w, p$ ) ~ 962
          ni
    end
end

```

FIG. 9

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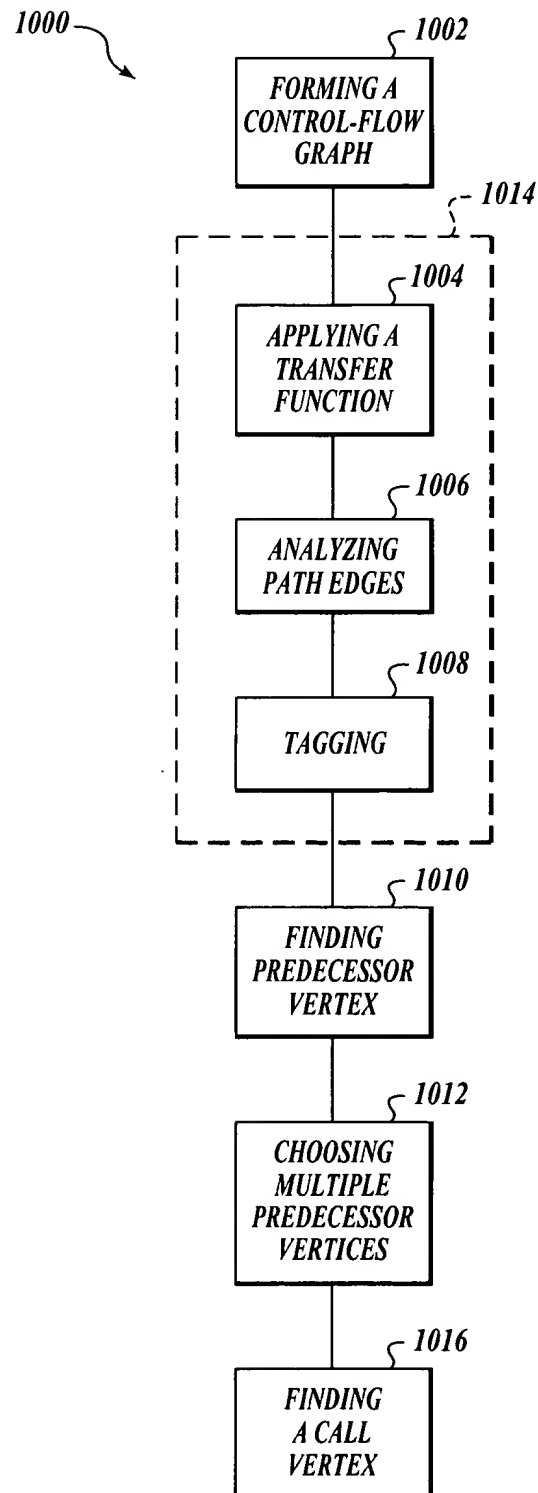


FIG. 10

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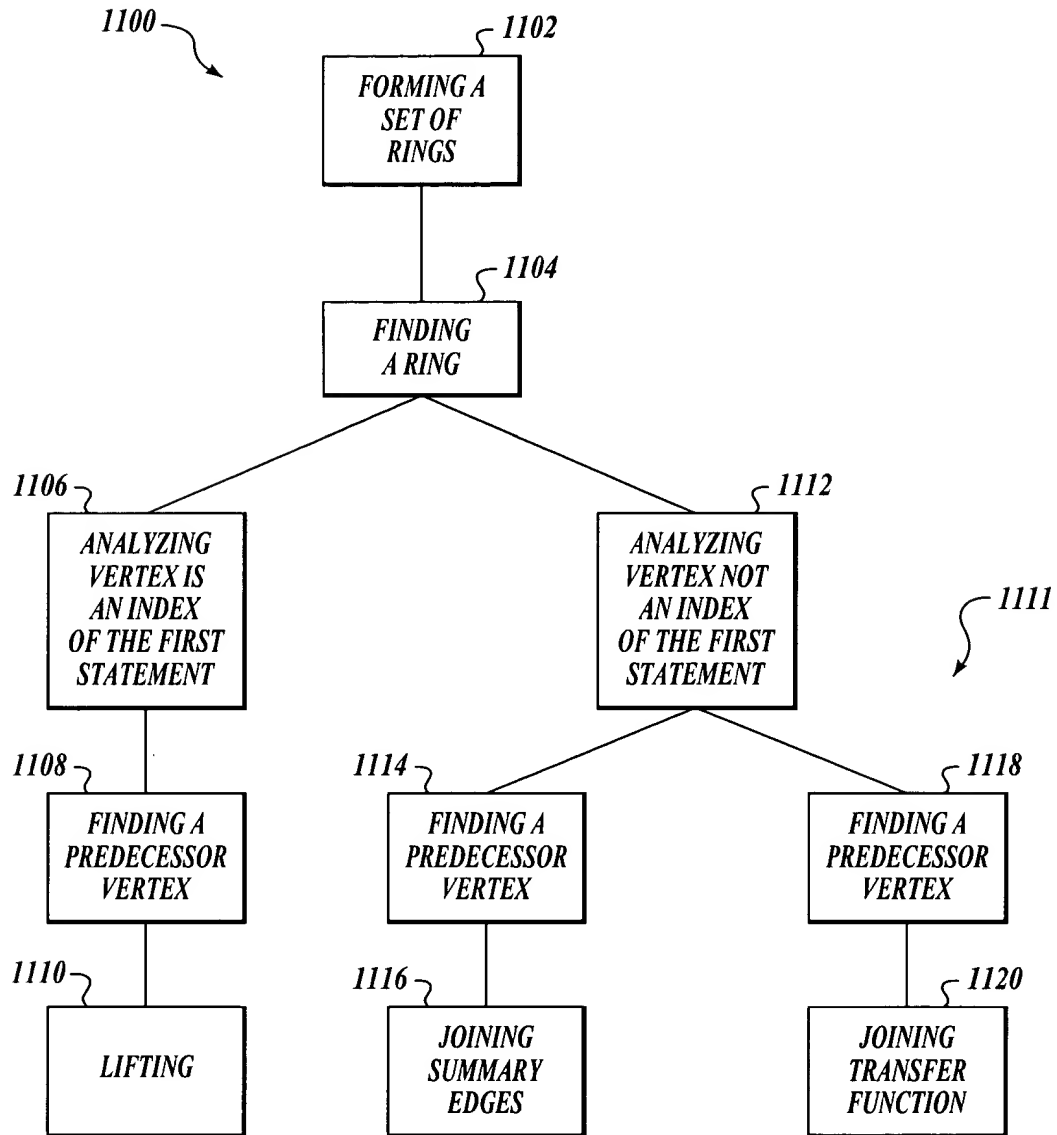


FIG. 11

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global

$PE' : V_G \rightarrow \text{set-of } (D \times D)$

$Worklist V_G \rightarrow \text{set-of } (D \times D)$

procedure Propagate($v : V_{G,p} : (D \times D)$)

begin

if $p \notin PE'(v)$ **then**

$PE'(v) := PE'(v) \cup \{p\}$

$Worklist(v) := Worklist(v) \cup \{p\}$

fi

end

procedure $CMOP_{SP_{rhs}}$ ($S : \text{set-of } D$)

begin

$PE'(\text{entry}) := \{\langle d, d \rangle \mid d \in S\}$

$Worklist(\text{entry}) := PE'(\text{entry})$

while $\exists v_2 \text{ s.t. } Worklist(v_2) \neq 0$ **do**

select and remove $\langle d_1, d_2 \rangle$ *from* $Worklist(v_2)$

for each $v_2 \rightarrow v_3 \in E_G$ **do**

for each $d_3 \in M(v_2 \rightarrow v_3)(\{d_2\})$ **do**

 Propagate($v_3 \langle d_1, d_3 \rangle$)

od

od

od

end

FIG. 12

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global

$PE' : V \rightarrow \text{set-of}(\text{set-of } D \times \text{set-of } D)$

$Worklist : V_G \rightarrow \text{set-of}(\text{set-of } D \times \text{set-of } D)$

procedure Propagate($v : V_{G,p} : (\text{set-of } D \times \text{set-of } D)$)

begin

if $p \notin PE'(v)$ **then**

$PE'(v) := PE'(v) \cup \{p\}$

$Worklist(v) := Worklist(v) \cup \{p\}$

fi

end

procedure $CSMOP_{SP_{rhs}}(S' : \text{set-of}(\text{set-of } D))$

begin

$PE'(\text{entry}) := \{\langle S, S \rangle \mid S \in S'\}$

$Worklist(\text{entry}) := PE'(\text{entry})$

while $\exists v_2 \text{ s.t. } Worklist(v_2) \neq 0$ **do**

select and remove $\langle S_1, S_2 \rangle$ *from* $Worklist(v_2)$

for each $v_2 \rightarrow v_3 \in E_G$ **do**

let $S_3 = M(v_2 \rightarrow v_3)(S_2)$ **in**

 Propagate($v_3 \langle S_1, S_3 \rangle$)

ni

od

od

end

FIG. 13